

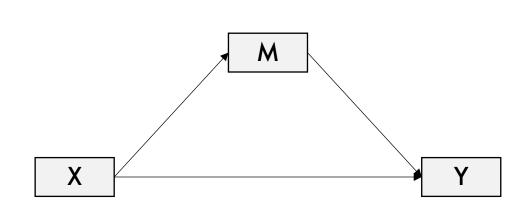
Trust the process? (Causal) Mediation analysis

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Slides: Resources

Foto von Apurv Das auf Unsplash

Mediation analysis as a causal inference problem

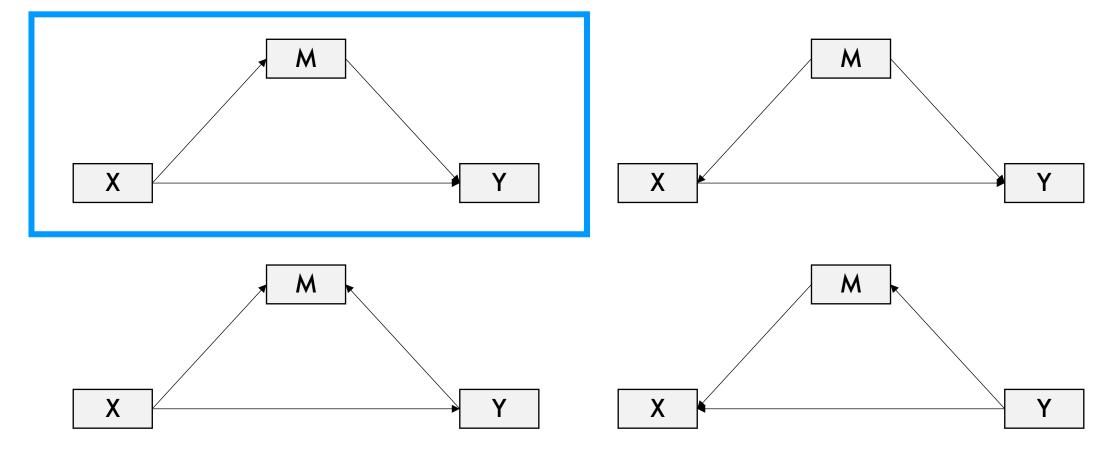


»Two central questions

- » To which extent does X affect Y via M? (Indirect effect)
- » To which extent does X affect Y apart from its effect via M? (direct effect)

»This is unambiguously a causal research question

» Baron & Kenny, 1986; MacKinnon, 2008; Preacher, 2015



In all of these scenarios we could fit a mediation model with M as a mediator of the effect of X on Y and find significant "direct and indirect effects."

Only in one of the scenarios could the estimates possibly have the desired interpretations (direct and indirect effects).

(If you don't desire that interpretation, you're not doing a mediation analysis but are instead for some reason investigating conditional associations)

(or really any causal analysis), Nguyen et al. (2020)

1. Definition

» Define the causal effects of interest

2. Identification

» Figure out the assumptions under which the effects of interest can actually be identified from the data (assuming that an infinite data were available)

3. Estimation

» Actually estimate the effects of interest (using only the available finite data)

(or really any causal analysis), Nguyen et al. (2020)

In the "traditional" mediation approach, this is a one-step procedure with a focus on estimation:

- The effects of interest are defined by the parameters of the statistical model.
 - 2. The identification assumption is essentially that the statistical model matches the actual model underlying reality.
- 3. Estimation via e.g. Baron & Kenny's (1986) three steps (not optimal), SEM (better), the regression-based approach implemented in PROCESS

(or really any causal analysis), Nguyen et al. (2020)

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The central point of contention

- »Mediation analysis rests on very strong identification assumptions which are likely to be wrong in many applications in psychology
 - » Bullock et al. (2010): Yes, but what's the mechanism? (Don't expect an easy answer)
 - » Fiedler et al. (2011): What mediation analysis can (not) do
 - » Rohrer et al. (2022): That's a lot to process! Pitfalls of popular paths models
 - » Blog posts: In psychology, everything mediates everything; Indirect Effect Ex Machina; Mediation analysis is counterintuitively invalid; That's a very nice mediation analysis you have there. It would be a shame if something happened to it.

2. Identification:

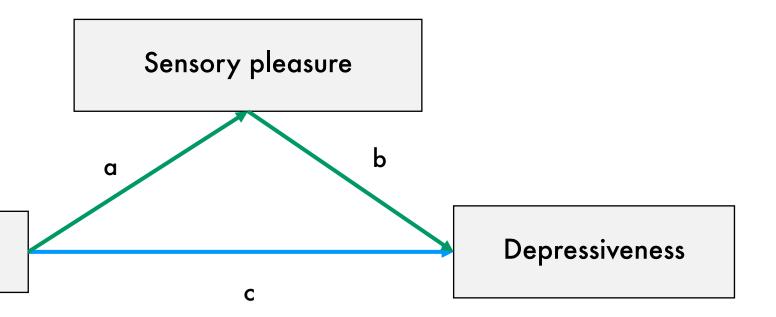
We need to be able to estimate the causal effects a, b, and c without any bias.

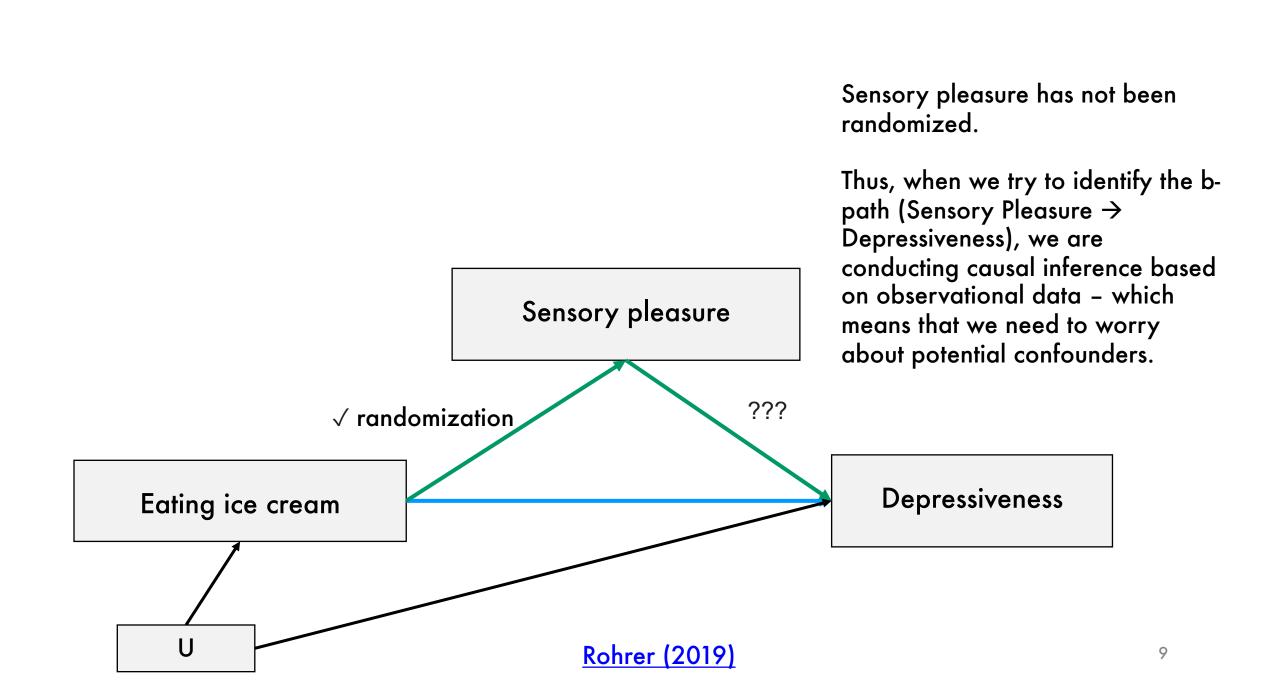
1. Definition of the causal effects:

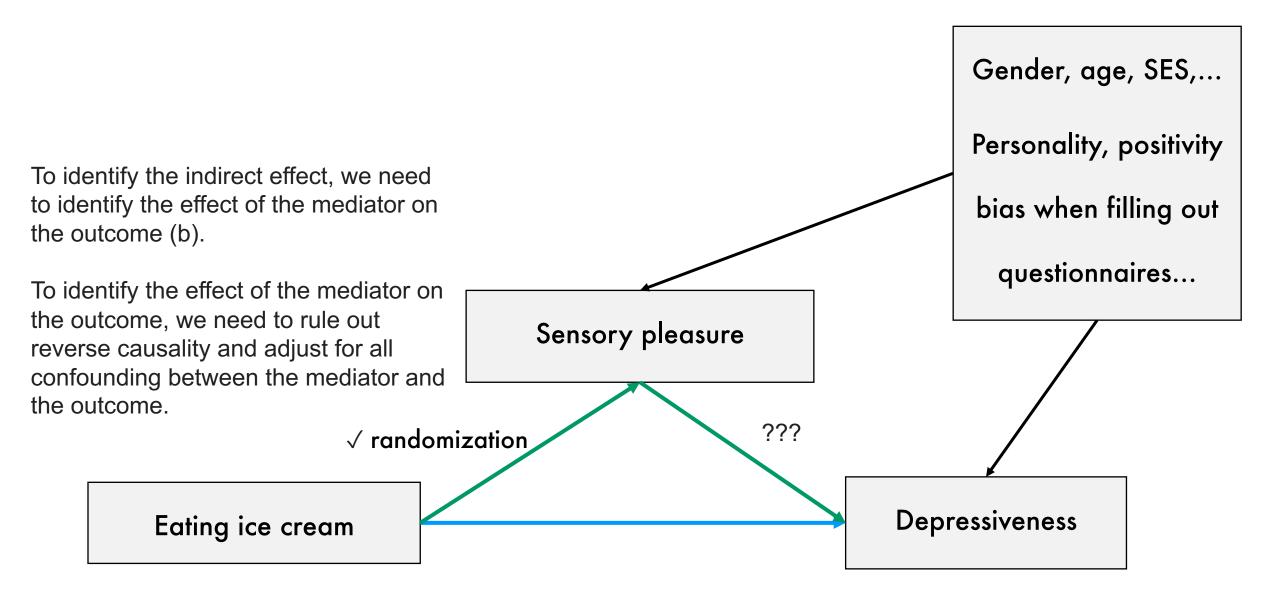
Indirect effect = a*b
Direct effect = c

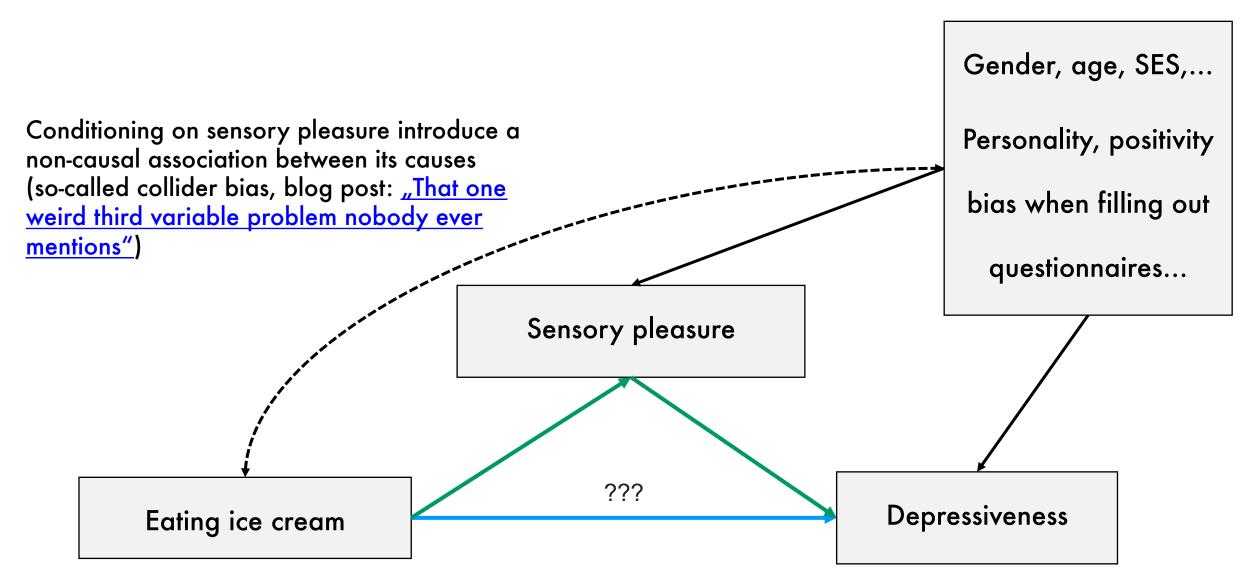
(Total effect = a*b + c)

Eating ice cream

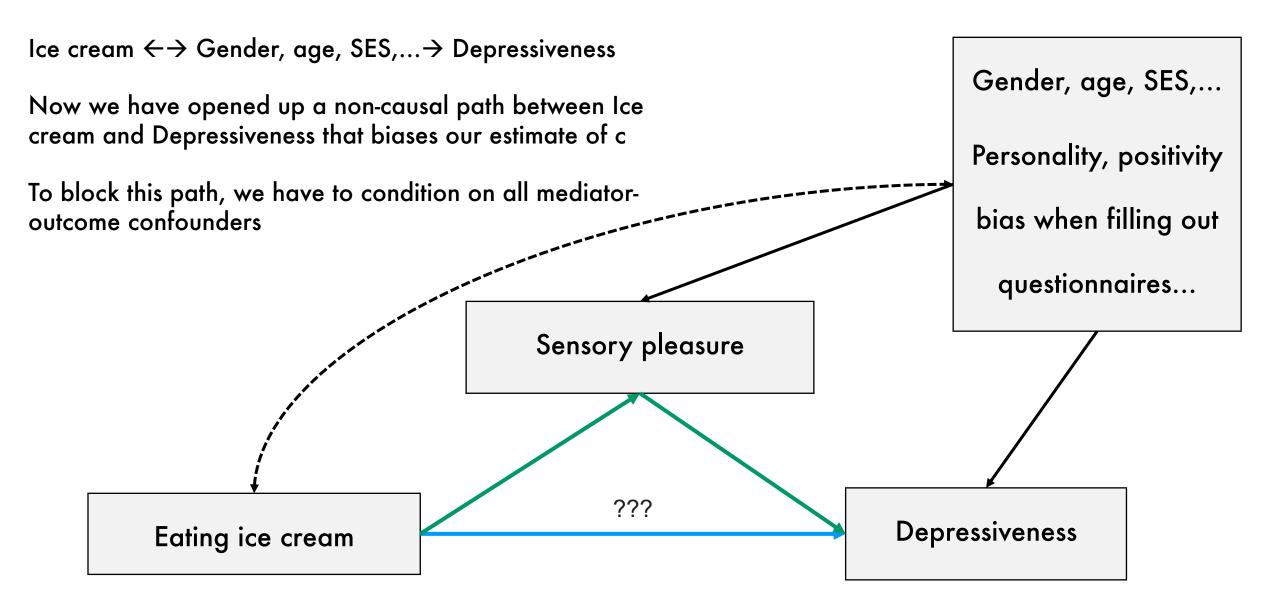








Ice Cream -> Sensory pleasure -> Depressiveness; block the indirect effect by conditioning on sensory pleasure Ice Cream -> Sensory pleasure <- Positivity bias etc. -> Depressiveness



Ice Cream -> Sensory pleasure -> Depressiveness; block the indirect effect by conditioning on sensory pleasure Ice Cream -> Sensory pleasure <- Positivity bias etc. -> Depressiveness

Identification assumptions of mediation analysis

- »In a nutshell, to identify both the indirect and the direct effect, we have to
 - » know all mediator-outcome confounders
 - » have measured them appropriately and
 - » have statistically adjusted for them appropriately (e.g., by including them as a covariate in our regression analyses, by including them in our SEM)
- » If the cause of interest (X) was not randomized, the same applies to any confounders between X and Y
 - » And X and M (these are a subset of the confounders between X and Y)

Identification assumptions of mediation analysis

- »These assumptions are usually not realistic in applications in psychology
 - » Both mediator and outcome are usually psychological variables which are potentially confounded by a myriad of other factors
- »One weird trick (Rohrer, 2019)
 - » Pick a mediator that is
 - » plausibly affected by $X (X \rightarrow M)$
 - » plausibly confounded with Y (M \leftarrow C \rightarrow Y)
 - » You now have good chances to get a significant (but spurious) indirect effect of X on Y via M, even if X does not affect Y at all

Identification assumptions of mediation analysis

- »The assumptions about no unobserved confounding apply to both the traditional approach and more modern "causal" appraoches
- »Additional assumptions in the traditional approach (indirect effect = a*b)
 - » Effect of M on Y does not depend on X (no treatment-mediator interaction; MacKinnon et al., 2020)
 - » The effects $X \rightarrow M$ and $M \rightarrow Y$
 - » Are the same for everyone or alternatively
 - » May vary, but do so independently (otherwise, the multiplicative logic does not work out)

"Causal" mediation analysis

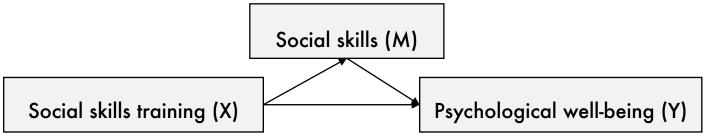
- »Causal because they are explicitly (and actively) being developed in the causal inference literature (e.g., <u>lmai et al., 2010</u>)
 - » The analysis goals are precisely as causal as the analysis goals of traditional mediation analysis
 - » All problems concerning potentially unobserved confounding still very much apply

"Causal" mediation analysis: Three steps

- » More focus on the precise definition of the effects of interest
- »Usually more awareness of the necessary identifiation assumptions
 - » (lack of unobserved confounding is usually assumed)
- » More flexible and varied estimation approaches
 - » Allowing e.g. for non-linear effects, treatment-mediator interactions etc.
 - » Implemented in various R packages

More precise definitions of (in)direct effects

Nguyen et al. (2020)



- » Counterfactuals in the individual-level (total) causal effects of X are simple
 - » Effect of X on Y for you: Your psychological well-being if you participated in the training minus your psychological well-being if you didn't participate in the training
 - » In potential outcomes notation: $Y^{X=1} Y^{X=0}$
- » But which potential outcomes are we considering when talking about direct and indirect effects?
 - » This will involve cross-world counterfactuals e.g., what if you received the training but your social skills did not change (e.g., what if the mediator remained constant?)

»Total effect = $Y^{X=1} - Y^{X=0} = Y^{X=1}$, $M(X=1) - Y^{X=0}$, M(X=0)



Your outcome
if you receive treatment
and
the mediator takes on the
value it takes on when you
receive treatment

Your outcome
if you do not receive
treatment
and
the mediator takes on the
value it takes on when you do

not receive treatment

(e.g., your well-being after the skills training if you have the social skills you'd naturally acquire from the training)

$$Total effect = Y^{X=1} - Y^{X=0} = Y^{X=1}, M(X=1) - Y^{X=0}, M(X=0)$$

» Natural direct effect =
$$Y^{X=1}$$
, $M(X=0)$ - $Y^{X=0}$, $M(X=0)$

Your outcome if you receive treatment and

the mediator takes on the value it the mediator takes on the value it treatment

Your outcome if you **do not** receive treatment and

takes on when you do not receive takes on when you do not receive treatment

(e.g., your well-being after the skills training if your social skills remain on the level if you did not receive the training)

> Contrast gives essentially the effect of "just" training, no skills acquired"

$$Total effect = Y^{X=1} - Y^{X=0} = Y^{X=1}, M(X=1) - Y^{X=0}, M(X=0)$$

» Natural direct effect =
$$Y^{X=1}$$
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» Natural indirect effect =
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Your outcome
if you receive treatment
and
the mediator takes on the value it
takes on when you do receive

treatment



the mediator takes on the value it takes on when you do not receive treatment



Contrast gives essentially the effect of "skills on top of training"

- »Total effect = $Y^{X=1} Y^{X=0} = Y^{X=1}$, $M(X=1) Y^{X=0}$, M(X=0)
- » Natural direct effect = $Y^{X=1}$, $M(X=0) Y^{X=0}$, M(X=0)
- » Natural indirect effect = $Y^{X=1}$, $M(X=1) Y^{X=1}$, M(X=0)
- »This is the direct-indirect composition
 - » We start from the control condition $Y^{X=0}$, M(X=0) and first add the direct effect to end up at $Y^{X=1}$, M(X=0), then add the indirect effect to end up in the treatment condition $Y^{X=1}$, M(X=1)

- »Alternatively we could do an indirect-direct composition and first add the indirect effect, then the direct effect
 - » Natural indirect effect = $Y^{X=0}$, $M(X=0) Y^{X=0}$, M(X=1)
 - » Natural direct effect = $Y^{X=0}$, $M(X = 1) Y^{X=1}$, M(X = 1)
- »The direct-indirect and indirect-direct composition will return different direct and indirect effects whenever there is a treatment-mediator interaction
 - » Essential question: does that interaction count toward the direct effect or toward the indirect effect?
 - » <u>VanderWeele (2014)</u> offers a unified decomposition into 4 components that keeps the interaction separate

»Which decomposition is the right one?

- » "Is there a mediated effect on top of whatever direct effect there is?": direct-indirect decomposition
- » "Is there a remaining direct effect on top of whatever indirect effect there is?": indirect-direct decomposition
- » When in doubt, both
- »In either case, we usually can only aim to estimate the averages of these individual-level direct and indirect effects

Less natural effects that can be estimated

- » Interventional (in)direct effects: Contrasting hypothetical interventions that fix treatment or mediator at specific values
 - » These do *not* decompose the total effect, but rather answer specific targeted research questions
 - » E.g., Sexual minority status → Bullying experiences → Depressive symptoms
 - » "What would be the effect of sexual minority status on depressive symptoms if we intervened so that the experience of bullying experiences among sexual minorities is the same as bullying experiences among majority members?"
 - » Controlled direct effects: Effect of X if we hold M constant at a certain level, e.g.: Effect of sexual minority status when we hold bullying experiences constant at "no bullying at all"

(or really any causal analysis), Nguyen et al. (2020)

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Identification assumptions in causal mediation analysis

- »Unfortunately, we still have to assume that all confounding has been adjusted appropriately
- »The specific assumptions depend on the effects of interest
 - » Total effect obviously the easiest one (randomization does the trick)
 - » Interventional effects (e.g., controlled direct effects) are harder
 - » Have to assume no unobserved mediator-outcome confounding
 - » Natural direct and indirect effects are the hardest
 - » Intermediate confounders are not allowed to exist

(or really any causal analysis), Nguyen et al. (2020)

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Estimation of causal mediation

- » This is essentially just an extension of how causal effects are estimated more generally
 - » Often combination of multiple models (model for the outcome mean Y, model for the mediator distribution M, model for the exposure assignment X)
- » Common approaches, both parametric and non-parametric
 - » Regression
 - » Weighting
 - » "Imputation", g-computation (Wang & Arah, 2015)
 - » See <u>Chatton & Rohrer (2024)</u> for a conceptual introduction to these approaches outside of the mediation context

Software!

mediation: R Package for Causal Mediation Analysis

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Harvard MIT Princeton Penn State Princeton

Abstract

In this paper, we describe the R package **mediation** for conducting causal mediation analysis in applied empirical research. In many scientific disciplines, the goal of researchers is not only estimating causal effects of a treatment but also understanding the process in which the treatment causally affects the outcome. Causal mediation analysis is frequently used to assess potential causal mechanisms. The **mediation** package implements a comprehensive suite of statistical tools for conducting such an analysis. The package is organized into two distinct approaches. Using the model-based approach, researchers can estimate causal mediation effects and conduct sensitivity analysis under the standard research design. Furthermore, the design-based approach provides several analysis tools that are applicable under different experimental designs. This approach requires weaker assumptions than the model-based approach. We also implement a statistical method for dealing with multiple (causally dependent) mediators, which are often encountered in practice. Finally, the package also offers a methodology for assessing causal mediation in the presence of treatment noncompliance, a common problem in randomized trials.

Keywords: causal mechanisms, mediation analysis, mediation, R.

CMAverse: a suite of functions for causal mediation analysis

About the Package

The R package CMAverse provides a suite of functions for reproducible causal mediation analysis including cmdag for DAG visualization, cmest for statistical modeling and cmsens for sensitivity analysis.

See the package website for a quickstart guide, an overview of statistical modeling approaches and examples.

Cite the paper: CMAverse a suite of functions for reproducible causal mediation analyses

We welcome your feedback and questions:

- Email bs3141@columbia.edu for general questions
- Email zw2899@cumc.columbia.edu for questions related to cmest_multistate

DAG Visualization

cmdag visualizes causal relationships via a directed acyclic graph (DAG).

Statistical Modeling

cmest implements six causal mediation analysis approaches including the regression-based approach by Valeri et al. (2013) and VanderWeele et al. (2014), the weighting-based approach by VanderWeele et al. (2014), the inverse odd-ratio weighting approach by Tchetgen Tchetgen (2013), the natural effect model by Vansteelandt et al. (2012), the marginal structural model by VanderWeele et al. (2017), and the g-formula approach by Robins (1986).

cmest currently supports a single exposure, multiple sequential mediators and a single outcome. When multiple mediators are of interest, cmest estimates the joint mediated effect through the set of mediators. cmest also allows for time varying confounders preceding mediators. The two causal scenarios supported are:

What about design based solutions?*

*Disclaimer: I have not kept up with that literature

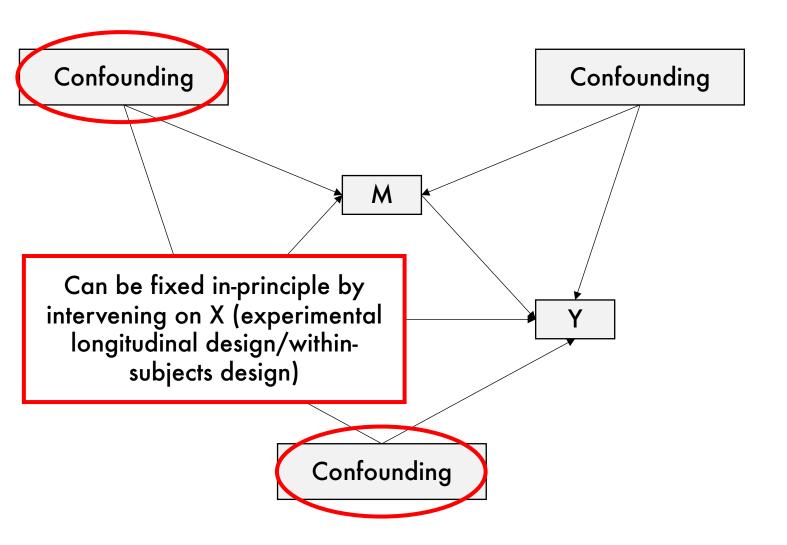
Design-based solutions

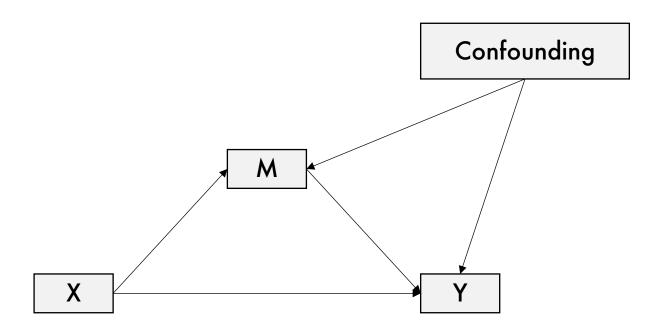
- »longitudinal data
- »intervening on X and on the mediator
 - » sequentially
 - » or simultaneously

Longitudinal data

»do not automatically solve confounding, <u>see Rohrer & Murayama (2023)</u>

»can rule out certain types of confounding if analyzed properly





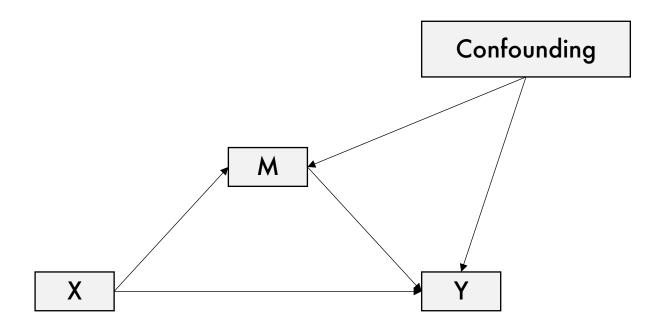
Confounding comes in "two types"

Time-invariant confounding:

- stable factors that uniformly affect M and X over the course of the study
- e.g., participants' gender, socioeconomic status, education, stable personality traits and other dispositions...
- what's time-invariant will depend on the duration of the study (stable over hours vs. days vs. years)

Time-varying confounding:

- fluctuating factors that can change within a person, or whose effects may change over time
- e.g., mood, health, any form of psychological state, current living situation



Opportunity afforded by longitudinal data: Compare people with themselves over time (within-subject analysis)

- → If we compare people to themselves, they are perfectly "matched" on time-invariant confounders
- → time-invariant confounders cannot "explain away" the observed within-subject associations

Confounding comes in "two types"

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Time-varying confounding:

- fluctuating factors that can change within a person, or whose effects may change over time
- e.g., mood, health, any form of psychological state, current living situation

Longitudinal data

»can rule out time-invariant confounding

- » if analyzed properly, rules of thumb:
 - » in multilevel analyses, you want a fixed effects model or some variation (including person ID as a categorical predictor [not just random intercepts!], within-subject centering, Mundlak device [person-specific mean of the cause of interest as additional predictor])
 - » in a SEM context, you can get away with random intercepts as long as they are allowed to correlate

Longitudinal data

- »can rule out time-invariant confounding
- »you still need to worry about time-varying confounding
 - » could there be things that change over time within people that confound their M with their Y?
 - » If yes, these would need to be additionally controlled for
- »"maximal" design-based approach here: repeated withinsubject experimentation

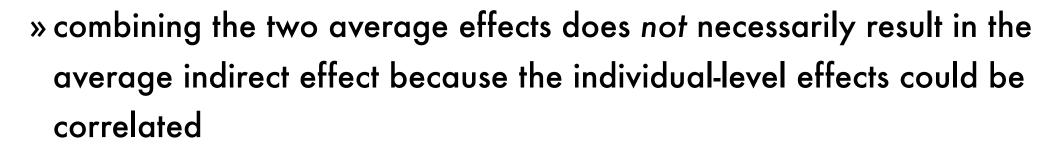
Design-based solutions

- »additionally intervening on the mediator (either sequentially or simultaneously)
 - » if that is an option at all specific problems arise when trying to manipulate for example psychological mediators (<u>Eronen, 2020</u>)
 - » assumptions are still needed to chain together the estimated effects, <u>Imai, Keele & Tingley (2010)</u>

Sequential interventions

First experiment identifies the average effect of X on M

Second experiment identifies the average effect of M on Y, possibly in the same people



X

» Scenario 1: X has an effect on M in half of the people; M has an effect on Y in only the other half of people → a and b are non-zero but the indirect effect is zero

M

» Scenario 2: X has an effect on M in half of the people; M has an effect on Y in only the same half of people \rightarrow a and b are non-zero; the indirect effect is *larger* than if one just multiplied the average effects

Person	a	b	a*b
1	1	0	0
2	1	0	0
3	0	1	0
4	0	1	0
Average	0.5	0.5	0

Person	a	b	a*b
1	1	1	1
2	1	1	1
3	0	0	0
4	0	0	0
Average	0.5	0.5	0.5

Sequential interventions

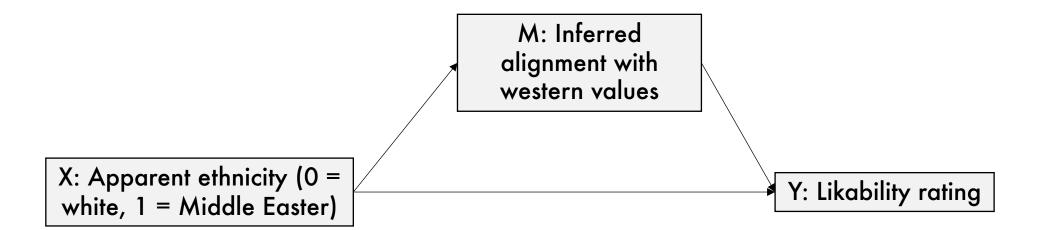
- » "maximal" design-based approach: intervene on X and on M repeatedly in the same people
 - » this way, you can estimate person-specific average effects (averaged over time) of $X \to M$ and $M \to Y$
 - » these can be combined to estimate person-specific average indirect effects
 - » necessary assumptions (I think): no time-varying intermediate confounders (mediator-outcome confounders affected by X); person-specific causal homogeneity over the observed window (causal parameters don't change over time)

Simultaneous interventions

- » e.g.: Manipulate X, additionally use some intervention to block indirect effect in some people (keep M from changing, set M to fixed level...)
 - » if there is a (positive) indirect effect, then the effect of X on Y should be larger if the indirect effect isn't blocked
- »this will obviously involve assumptions for example, that we can block the indirect effect without changing the nature of the manipulation of X
- » Ge (2023): Experimentally manipulating mediating processes

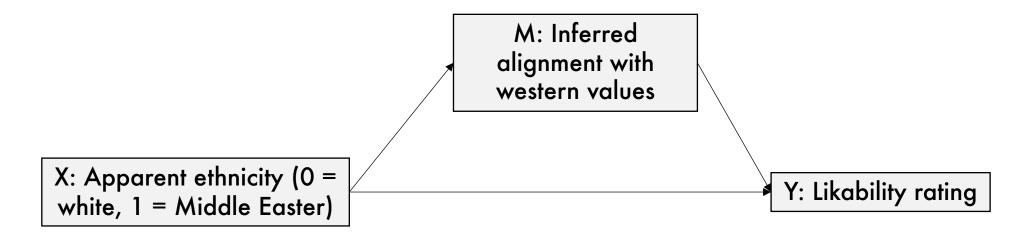
Simultaneous interventions

- » In my (limited) review experience, researchers get confused when they try to map the mediation logic onto experimental interventions in the abstract
- » I'd thus recommend to *initially* reason about this in terms of experimental design and hypotheses rather than in terms of mediation analysis
 - » "If X affects Y via M, then if we do the following, we expect the following outcome..."
 - » Makes better use of existing intuitions about threats to validity (which point towards necessary assumptions)
 - » can still map onto mediation logic in the next step to more formally check whether you got everything right



2 x 3 design:

- image of white or Middle Eastern person (manipulates X)
- additional information meant to manipulate M
 - none (M = "natural" value for X)
 - target volunteers for Amnesty international (M = high)
 - target volunteers for the Salafists (M = low)



"Natural"			Amnesty International		Salafists	
White	YX = 0, M(X = 0)		Y X = 0, M = high		Y X = 0, M = low	
Middle Eastern	YX = 1, M(X = 1)		Y X = 1, M = high		Y X = 1, M = low	
	Comparison vields total effe	ct y	Comparison rields controlle direct effect	d	Comparison yi different contro direct effect	

We are not estimating natural effects here because we force certain values upon the mediator
→ we are not in the business of decomposing the total effect into additive parts

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	"Natural"		Amnesty International		Salafists	
White	YX = 0, M(X = 0)		Υ X = 0, M = high		Y X = 0, M = low	
Middle Eastern	YX = 1, M(X = 1)		Υ X = 1, M = high		Y X = 1, M = low	

Total effect ≈ Controlled direct effect → speaks against mediation

Total effect > Controlled direct effect → speaks in favor of mediation*

Total effect < Controlled direct effect → Could actually happen, (e.g., M*X interaction)

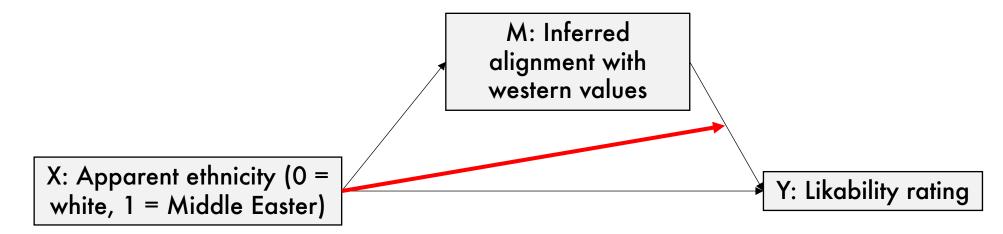
More precise conclusions will hinge on additional assumptions

Controlled direct effect $\approx 0 \rightarrow$ full mediation?

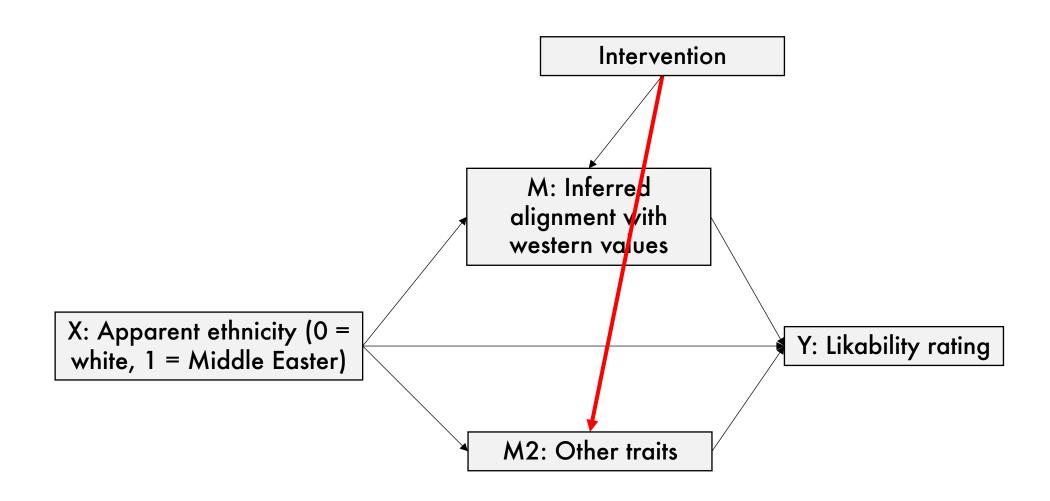
"Threat to validity" of this conclusion:

- Volunteering for AI may mean different things depending on X
 - X = 0: not that extraordinary, X = 1: may speak to a special commitment/motivation
- M = high may thus give X = 1 a huge likability boost, which hides an existing direct effect
- at least 3 different ways to conceptualize this from a causal inference perspective

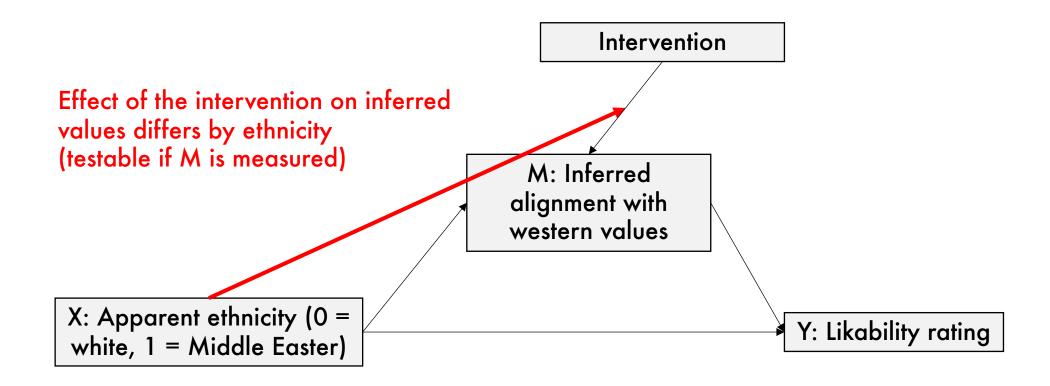
^{*}see Ge (2023) for additional conditions (X affects measured M in the "natural" group, manipulation of M successfully changes measured M)



Treatment-mediator interaction: Effect of inferred values depends on apparent ethnicity



Intervention affects another (possibly unobserved) mediator



	"Natural"		Amnesty International		Salafists	
White	YX = 0, M(X = 0)		Υ X = 0, M = high		Y X = 0, M = low	
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More precise conclusions will hinge on additional assumptions

Controlled direct effect $\approx 0 \rightarrow$ full mediation?

"Threat to validity" of this conclusion:

- Volunteering for AI may mean different things depending on X
 - X = 0: not that extraordinary, X = 1: may speak to a special commitment/motivation
- M = high may thus give X = 1 a huge likability boost, which hides a remaining direct effect
- different ways to conceptualize this from a causal inference perspective

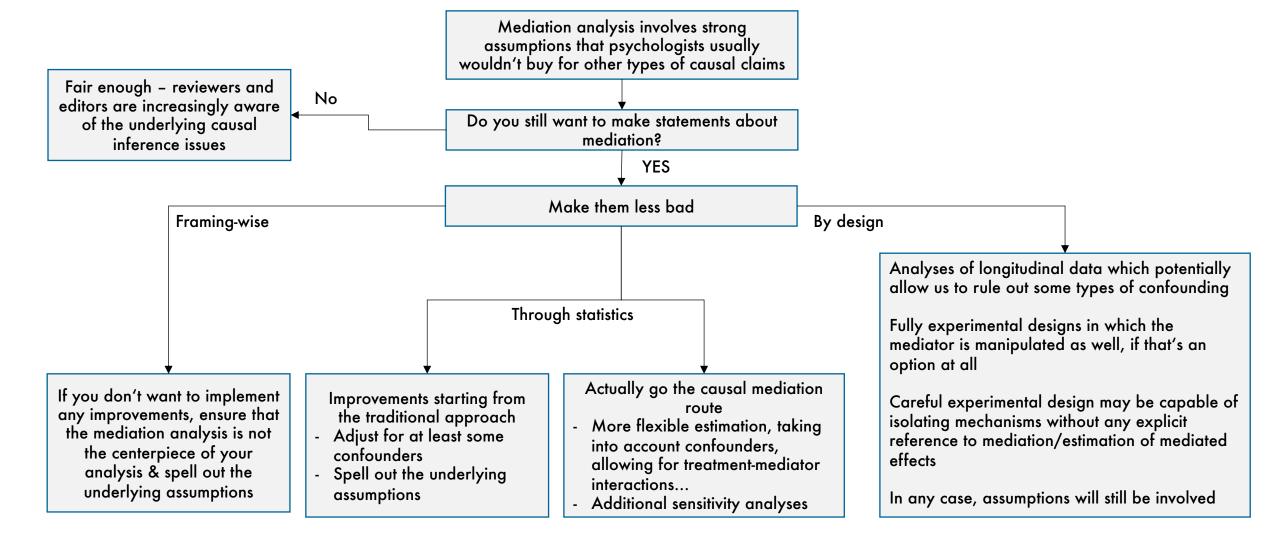
These threats to validity must be assumed away to warrant the conclusion of full mediation



Matthay & Glymour (2020): A Graphical Catalog of Threats to Validity

Gabriel et al. (2025): Elucidating some common biases in randomized controlled trials using directed acyclic graphs

Okay, so that was a lot



Thank you for your attention!

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Slides: Resources